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## CHANGES IN THE GEOMETRY AND VOLUME OF RABOTS GLACIÄR, SWEDEN, 2003–2011: RECENT ACCELERATED VOLUME LOSS LINKED TO MORE NEGATIVE SUMMER BALANCES

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ABSTRACT. Terminus geometry, ice margins, and surface elevations on Rabots glaciär were measured using differential GPS during summer 2011 and compared with those similarly measured in 2003. Glacier length over the eight years decreased by ~105 m corresponding to 13 m  $a^{-1}$ , a rate consistent with ice recession over the last several decades. Measured changes in surface elevations show that between 2003 and 2011 the glacier's volume decreased by ~27.6  $\pm$  2.6  $\times$  10<sup>6</sup> m<sup>3</sup>, or 3.5  $\pm$  0.3  $\times$  10<sup>6</sup> m<sup>3</sup> a<sup>-1</sup>. This compares favorably with an estimate of  $-28.1 \pm 2.6 \times 10^6 \text{ m}^3$ based on a mass-balance approach. The rate of volume loss appears, however, to have significantly increased after 2003, being substantially greater than rates determined for the intervals 1959-80, 1980-89, and 1989-2003. This increase corresponds to a sustained interval of more negative summer balances. Previous work suggests that as of 2003 Rabots glaciär had not yet completed its response to a ~1°C warming that occurred c. 1900, and thus the current marked increase rate of ice loss might reflect the effect of recent, or accelerated regional warming that occurred during the last decade superimposed on its continued response to that earlier warming.

*Key words*: glacier, climate, mass balance, dGPS, Rabots glaciär, northern Sweden

#### Introduction

Given the paucity of meteorological records, glaciers in high, northern latitudes are particularly important indicators of regional climate change (Dowdeswell *et al.* 1997; Dyurgerov and Meier 2000; Lemke *et al.* 2007) and their retreat is recognized as making a significant contribution to current sea-level rise (Meier *et al.* 2007; Radić and Hock 2011; Gardner *et al.* 2011). There is, however, an insufficient number of long-term, continuous (i.e. annual, or nearly so) measurements of recent glacier change and/or mass balance to fully understand the impact of a changing climate on the Arctic cryosphere; specifically there exists a need for increasing the geographic coverage and extending the time series of such measurements (Dyurgerov and Meier 2000; Lemke et al. 2007; Zemp et al. 2009). Consequently geodetic measurements of glacier surfaces, typically repeated over multiyear intervals, have become increasingly useful to document global and regional changes in ice volume and mass (e.g. Cogley 2009; Nuth et al. 2010). These measurements afford a better assessment of glacier response to climate change than do, for example, records of glacier length variations because of the various factors that can influence the behavior of the glacier's terminus. Geodetic measurements have also been useful for reconstructing annual massbalance variations (Vincent 2002) and for evaluation of uncertainties associated with the direct, or glaciological method of balance measurement or vice versa (Krimmel 1999; Cogley 2009; Zemp et al. 2010). Moreover, even in those regions where long-term records exist (e.g. northern Scandinavia), such measurements could help resolve the ambiguity resulting from disparate glacier behavior within a restricted geographic area (Brugger 2007) in order to better assess and clarify the impact of climate change.

In this paper we present the results of a second differential GPS (dGPS) survey undertaken in 24–29 Jul., 2011 to determine the changes in the geometry and volume of Rabots glaciär that have occurred since the first dGPS survey carried out in 17–21 Jul., 2003 (Brugger *et al.* 2005). In addition to building on a long observational record (going

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back slightly more than 100 years), we compare our results with volume changes calculated using a record of annual mass-balance variations for the same period. We then briefly discuss the changes in geometry in the context of the glacier's shorter- and longer-term behavior, and mass balance variations driven by ongoing climate change.

#### Physical setting and recent glacier behavior

Rabots glaciär (67°55'N, 18°30'E) is located in the Kebnekaise Massif in northern Sweden (Fig. 1) and as of 2011 had an area (planar) of about 3.4 km<sup>2</sup>. Like others in northern Sweden, the glacier advanced late in the nineteenth century during the local culmination of the Little Ice Age (LIA) (Karlén 1973; Holmlund 1993), and then began to retreat in response to a regional warming of ~1°C for, both annual and summer temperatures that

began c. 1900 and continued into the mid-1930s (Holmlund 1993; Klingbjer and Moberg 2003; Klingbjer et al. 2005). Sporadic observations and/or measurements of the glacier's terminus position were made between 1883 and 1981 [e.g. Rabots, 1900; Svenonious, 1910; Karlén 1973; Holmlund and Schytt 1987; unpublished reports, land and aerial photographs (especially F. Enqvist's 1910 photos), and maps] after which more systematic glaciological studies began (Brugger 1992, 2007; Brugger et al. 2005; published annual reports and unpublished data from the nearby Tarfala Research Station). Since 1981 an almost continuous mass-balance record exists (available from the World Glacier Monitoring Service, http:// www.wgms.ch, 5 Aug., 2014). Compiling many of the measurements, Brugger et al. (2005) quantified changes in the geometry and volume of Rabots glaciär for the interval 1910-2003. Specifically they



Fig. 1. Location map of Rabots glaciär (inset) and the glacier surface in 2011. Dotted line is the 2003 ice margin. Filled circles show locations of dGPS measurements, some obscured by contours or the line indicating the ice margin. Squares show points obtained by interpolation and photo analyses used to augment the survey data. Coordinate system is RT90 2.5 gon and glacier contour interval is 25 m.

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show that following an initial sluggish retreat of  $\sim 2.0 \text{ m a}^{-1}$ , ice recession increased to a relatively constant rate, within the resolution of the observations, of 10.1 m a<sup>-1</sup> (standard deviation,  $\sigma =$  $\pm 2.6 \text{ m a}^{-1}$ ) between 1933 and 2003. Although changes in glacier volume during this time were more difficult to assess owing to temporally sparse data, significant ice loss apparently began prior to 1959. For the period 1959–2003 glacier volume had decreased by  $75.9 \times 10^6 \text{ m}^3$ , however the rate of volume loss shows a steady decrease from  $\sim 2.4 \times 10^{6} \text{ m}^{3} \text{ a}^{-1}$  between 1959 and 1980,  $\sim 1.2 \times 10^{6} \text{ m}^{3} \text{ a}^{-1}$  $10^{6} \text{ m}^{3} \text{ a}^{-1}$  between 1980 and 1989, to ~1.0 × 10<sup>6</sup> m<sup>3</sup> a<sup>-1</sup> between 1989 and 2003. Regional increases in winter precipitation and its effect on glacier mass balance (Pohjola and Rogers 1997; Fealy and Sweeney 2005; Kohler et al. 2006) might provide an explanation for the decreasing rate of volume loss. Nevertheless while slowing, volume loss continued to be significant up to 2003, leading Brugger et al. (2005) to conclude that Rabots glaciär had not yet completed its response to the earlier climatic warming, presumably due to the glacier's long response time (discussed subsequently) quantified as either a volume timescale (Jóhannesson et al. 1989) or as a length response time (Oerlemans 2001). Given the potential competing influences of increased winter precipitation and more recent, or accelerated warming in the region (Klingbjer and Moberg 2003; Callaghan et al. 2010) on the mass balance of Rabots glaciär, a remaining question is how these are manifest in changes in glacier length and volume post-2003.

#### Methods

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#### The 2011 dGPS survey

The 2011 dGPS survey used a real-time kinematic technique that was identical to that used in 2003 (carried out 15-21 Jul.). A base station receiver (Trimble 4600LS) was located at a fixed point (I-63 on Fig. 1) on the crest of a moraine ~0.5 km from the ice margin. That fixed point was surveyed in 2003 and those coordinates were entered as the precise location for the base, thus linking the two dGPS surveys. After initialization of the base station, the ice margin and surface elevations were surveyed by a backpack-mounted roving receiver. Points were measured individually (as opposed to continuously) to ensure that the height of the receiver above the glacier's surface was constant. Corrections to the rover's position were continuously broadcast in real time via radio link from the base receiver. At each location, three measurements were automatically made, averaged, and recorded. Quality control was preset to exclude measurements that exceeded 0.05 m in horizontal and vertical precision, however it should be noted that local surface irregularities (due to differential ablation, meltwater channels, etc.) could in places be several decimeters or more. We varied the density of the more than 1000 measurement locations (Fig. 1) according to where more significant changes in surface elevations or the ice margin were expected (e.g. the glacier's terminus) or where the local surface was more undulating and less planar. As in 2003, we were unable to measure points in the tributary cirques because of steep and/or crevassed glacier surfaces and the associated danger inherent in glacier travel. Measurements along the southern margin of the glacier's lower reach were also troublesome because the nearly vertical walls effectively blocked satellite signals. It was therefore necessary to augment the survey data by observations of glacier change in these areas as described subsequently. During both the 2003 and 2011 surveys more than 97% of all dGPS measurements were made directly on the ice surface, summer melting having been well underway and quite extensive by the dates of these surveys. (This is reflected in the summer balances for 2003 and 2011 that were -2.27 and -2.11 m w.e., respectively, and substantially greater than the period average of 1.67 m w.e.)

In addition to those of the glacier surface and margin, several fixed (or control) points were measured to facilitate georeferencing and comparison with the 2003 survey. The mean difference in elevation for these points was  $0.090 \pm 0.099$  m; all elevations measured in 2011 were lower. It should be noted, however, that for the most stable fixed points surveyed (II-63, a large boulder on a flat moraine crest, and F-1 on bedrock; Fig. 1) the differences were only 0.028 and 0.075 m, respectively. The other points were either marked boulders in the glacier's forefield resting on sometimes (less stable) saturated or frozen fine-grained outwash sediments, or in one case an older fixed point established on loose, steeply dipping bedrock so that some subsidence and/or movement may have occurred to these points in the intervening eight years. This is also suggested by changes in horizontal positions that can be as much as 0.14 m as opposed to  $\sim 0.01 \text{ m}$  for the more stable points. Therefore given the small differences in the elevation measurements, especially those for II-63 and F-1, and the magnitude of irregularities in the glacier surface, no attempt was



Fig. 2. An example of the photo comparisons used to assess changes in the ice margin in those areas where dGPS surveying could not be carried out due to dangers of glacier travel or lack of satellites. Shown here is part of the southeastern cirque. Arrows show several of the common points used in this comparison. Resolution on originals is far better than that shown here and we estimate that elevation differences greater than  $\sim 1$  m could be detected.

made to correct for the slight apparent discrepancies in fixed point elevations between the 2003 and 2011 surveys.

#### Augmentation and analysis of survey data

Supplementary data for those areas where surveying was not possible were obtained by comparing terrestrial photographs from 2003 with those from 2011 (Fig. 2). This was done visually, i.e. we did not perform any ortho-rectification of the photographs. In this way a quantitative assessment was made of the changes in both the position and elevation of the ice margin during this interval. Photographic coverage allowed changes greater than ~1 m to be assessed for virtually all of the unmeasured ice margin (Fig. 1) and we note that where revealed by photos very little change occurred. Where the change was more significant, estimates of the coordinates and elevation of the new ice margin were obtained using the 2003 digital elevation model (DEM) and extrapolating the local bedrock slope. Simple linear interpolation of elevation changes was used between the ice margin and the nearest surveyed points with due consideration of persistent trends in surface topography as revealed by maps and photographs. Nowhere was there any indication of thickening. It should be noted that more often than not no discernable changes occurred in the ice margin in these areas while thinning nearby was obvious, but modest. [For comparison, Koblet et al. (2010) made a similar observation regarding changes in the accumulation area of nearby Storglaciären.] This could suggest a non-linear lowering of the glacier surface, implying that our interpolation scheme underestimates volume losses in these areas.

The 2011 survey and supplemental data were imported into Surfer (Golden Software) to create a DEM and a contour map of Rabots glaciär. Kriging was used for interpolation to determine glacier surface elevations on nodes over a regular  $10 \times 10$  m grid. Examination of variograms suggested that interpolation using a linear kriging without a nugget effect was appropriate. This explicitly assumes that both measurement error and elevation changes over the relevant distance scale(s) (i.e. nearest neighbors) are small, microtopographic roughness notwithstanding, making the gridding method an exact interpolator.

#### Results

#### Ice extent and retreat 2003–2011

The glacier's area in 2011 was  $3.43 \times 10^6$  m<sup>2</sup>, a reduction of  $2.6 \times 10^5$  m<sup>2</sup> (7%) over its 2003 extent (Table 1). The most pronounced changes occurred not only at the terminus but also along the northern margin (Fig. 1). This is not surprising because the southern margin serves as part of the glacier's accumulation area as the steep valley walls enhance snow accumulation through avalanching and possibly wind drift, and reduce solar radiation hence ablation (Brugger 1992). The most significant uncertainties in defining the glacier areas stem from the inability to identify the ice margin where it was obscured by morainal or other debris, both during surveying and in analyzing photographs. This was

Table 1. Measured changes in the geometry and volume of Rabots glaciär 1910–2011. A is glacier area,  $\Delta A$  is the change in area,  $\Delta h$  is the mean thickness change,  $\Delta V_m$  is the change in glacier volume based on measured changes in surface elevations, and dV/dt is the rate of volume change.

Year	Retreat <sup>a</sup> rate (m)	Retreat (m a <sup>-1</sup> )	$A^*$ (10 <sup>6</sup> m <sup>3</sup> )	ΔA (%)	$\overline{\Delta h}$ (m)	$\Delta V_m^{\dagger}$ (10 <sup>6</sup> m <sup>3</sup> )	dV/dt (10 <sup>6</sup> m <sup>3</sup> a <sup>-1</sup> )
1910	0		4.57				
1933	45	2.0					
1946	197	11.7					
1952	234	6.2					
1959	270	5.1	4.12	-9.8			
1968	358	9.8					
1975	432	10.6					
1980	498	13.2	3.82	-7.3	$-12.4 \pm 1.5$	$-51.1 \pm 6.0$	-2.43
1984	533	8.8					
1989	589	11.2	3.75	-1.9	$-2.7 \pm 1.9$	$-10.4 \pm 7.0$	-1.16
1998	692	11.4					
2003	750	11.6	3.69	-1.4	$-3.9 \pm 1.9$	$-14.4 \pm 7.0$	-1.03
2011	855	13.1	3.43	-7.0	$-7.3 \pm 0.7$	$-27.6 \pm 2.6$	-3.45

\* Referenced to the 1910 maximum LIA extent.

<sup>†</sup> Data for 1959, 1980, 1989, and 2003 from Brugger et al. (2005).



Fig. 3. Ice margins and retreat of Rabots glaciar 1910–2011. Greyed area shows the ice extent in 1910. (After Brugger et al. 2005.)

particularly problematic at the southern part of the terminus and mid-reach along the northern margin. In the latter, it was also often difficult to distinguish between (semi-)perennial snow patches and glacier ice. To address these issues, we drew several reasonable alternatives to the ice margins depicted in Fig. 1 and measured glacier area. All areas fell within 1% of one another and we subsequently used this as the uncertainty.

The 2011 terminus geometry is shown in Fig. 3 that documents ice recession from the glacier's LIA

maximum bracketed between 1910 and 1916 (Karlén 1973). [The earlier date is based on the Enqvist photographs but it remains unclear why 1916 was chosen as the older date (P. Holmlund, pers. com., 8 Jan., 2013). For consistency with previous works (Brugger *et al.* 2005; Brugger 2007) we use 1910 when referring to the date of the LIA maximum.] Glacier length between 2003 and 2011 decreased ~105 m based on an average of the difference in 2003 and 2011 terminus positions taken from six lines equally spaced over about 500 m of

the glacier's front, this approach being consistent with measured length changes reported by Brugger *et al.* (2005). Because of the precision of the dGPS methodology we assigned an uncertainty of around  $\pm 1$  m for the measured distances that is largely due to limitations in plotting the survey data and measuring on that plot. The mean rate of retreat for this interval was ~13.1 ± 0.1 m a<sup>-1</sup>.

#### The 2011 glacier surface

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Figure 1 shows the contoured glacier surface for Rabots glaciär in 2011 from the constructed DEM. To assess the quality of the interpolation, five random samples of 100 surveyed point elevations were compared with interpolated values. The mean residual (difference) in elevations for these samplings was in all cases less than 0.20 m. Residuals were normally distributed (standard deviations  $\leq -2.0$  m), and thus interpolated values are equally likely to slightly underestimate as overestimate surface elevations. We thus assumed an uncertainty of 0.2 m for the glacier surface where elevations were measured. If, as noted above, in those areas where measurements could not be made, surface lowering followed a nonlinear trend (e.g., fitted using a second-order polynomial); thinning in these areas might be underestimated by ~1 m. Considering that these are approximately one-third of the glacier's total surface area in 2011, this placed a lower bound on the uncertainty (via weighting) associated with the surface of  $\sim 0.5$  m which we then took as the upper bound as well.

#### Changes in ice thickness and volume 2003–2011

Changes in ice thicknesses  $\Delta h$  were obtained by subtracting the 2003 DEM of the glacier surface elevations from those of 2011 (Fig. 4a). Mean thickness change  $\Delta h$  was -7.3 m. Based on the standard deviation ( $\sigma = \pm 5.5$  m), over most of the glacier the change in surface elevation was between -1.8 and -12.8 m. As expected the largest changes occurred near the terminus ( $\sim -27$  m) and over the lower reach of the glacier. Accordingly, the volume change  $\Delta V_m$  determined by measured changes in surface elevations between 2003 and 2011 was  $-27.6 \times 10^6$  m<sup>3</sup> corresponding to a mean rate of  $-3.5 \times 10^6$  m<sup>3</sup> a<sup>-1</sup> (Table 1).

The uncertainties in these estimates were difficult to precisely quantify for several reasons, perhaps the most obvious being the estimation of presumed thinning in the areas where dGPS measurements could not be made. We therefore evaluated the uncertainties in the following ways. An uncertainty of  $\pm 0.5$  m was used for the 2003 ice surface based on an analysis similar to that described above. Propagation of uncertainties in the surface elevations and in glacier area yields an uncertainty of  $\pm 0.7$  m (or  $\sim \pm 10\%$ ) for  $\overline{\Delta h}$  and  $\pm 2.6 \times 10^6$  m<sup>3</sup> for  $\Delta V_m$  (also  $\pm 10\%$ ).

When possible, we attempted to explicitly quantify the magnitude of potential errors that might be introduced as a result of our assumptions and/or methodologies in order to ensure that these fell well within the uncertainties stated above. First, even in the unlikely case that thinning in those areas that went unmeasured was underestimated by 2 m, an additional volume loss of  $\sim 2.2 \times 10^6$  m<sup>3</sup> might have occurred. Second, the kriging algorithm also resulted in several small areas where minor thickening is indicated (Fig. 4a), and this is most likely not the case. Eliminating those "offending" values by arbitrarily setting any positive  $\Delta h$  to zero changed  $\Delta V_m$  to  $-28.3 \times 10^6$  m<sup>3</sup>, a 3% change over our best estimate. Alternatively applying a low-pass filter (3  $\times$  3 Gaussian) to the gridded  $\Delta h$  values eliminated all positive values (Fig. 4b), making  $\Delta h = -7.6 \text{ m}$  and  $\Delta V_m = -28.7 \times 10^6 \text{ m}^3$ . Our uncertainty in  $\Delta V_m$  therefore encompasses those inherent in each of the foregoing as well as accounting for irregularities in the glacier surfaces, measurement inconsistencies (e.g. lean of roving receiver pole), slight differences in the 2003 and 2011 dGPS elevations of control points, and/or instrumental error.

#### Discussion

## *Comparison of geodetic and glaciological mass balances*

Systematic measurement of the mass balance of Rabots glaciär using the glaciological methods began in 1981 and continues to the present, but details of the measurement protocols used over this period have varied. Currently about 100 probings are made for measuring accumulation (winter balance) and several (5–10) ablation stakes are monitored to determine the summer balance (P. Jansson, pers. com., 8 Aug., 2012). It is therefore important to evaluate the effectiveness of the ongoing mass-balance program. We do this by comparing geodetic and glaciological (mass balance) derived volume changes for the interval 2003–11.

Unfortunately at the time of this writing, massbalance data for the years 2003–04 and 2006–07 are



Fig. 4. Image map showing the changes in glacier surface elevations 2003-2011 using (a) unfiltered gridded data and (b) after applying a  $3 \times 3$  Gaussian filter.

not available. However, a good correlation exists between the glacier-wide, annual mass balance  $b_n$  of Rabots glaciär and that of nearby Storglaciären  $(n = 29, r^2 = 0.75, p < 0.001)$  that then allows variations in  $b_n$  for Rabots glaciär to be filled in and/or extended, albeit crudely, back to 1946 (Fig. 5a, b). Using this composite record the volume change based on mass-balance variations between 2003 and 2011 is calculated by

$$\Delta V_b = \frac{1}{\bar{\rho}} \sum_{i=2003}^{2011} b_{n_i} A_i$$
 (1)

where  $\overline{\rho}$  is the mean density of mass (snow and/or ice) lost or gained during the balance year *i*,  $A_i$  the glacier area, and  $b_{n_i}$  the glacier-wide annual mass balance. The density is weighted quantity based on the areal distribution of snow/firn (~550 kg m<sup>-3</sup>)

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and ice (916 kg m<sup>-3</sup>) over the glacier's extent using an equilibrium-line altitude that can be related to the annual mass balance by correlation (n = 21,  $r^2 = 0.76$ , p < 0.001), and hence accumulation area



Fig. 5. (a) Correlation of measured specific net mass balances  $b_n$  for Rabots glaciär and Storglaciären (n = 29,  $r^2 = 0.75$ , p < 0.001) and (b) the extended record of variations of  $b_n$  for Rabots glaciär for 1946–2011 based on measured values (solid circles) and estimates (open circles) using the regression equation in (a). Mass-balance data are from unpublished updated compilations provided by P. Jansson (personal communication, 2012).

via hypsometry. Snow/firn density is based on (1) measurements which show that although typical snow densities range from ~350 to 400 kg m<sup>-3</sup> at the approximate end of the accumulation season they increase to ~400–550 kg m<sup>-3</sup> very early in the ablation season (unpublished reports of the Tarfala Research Station); and (2) a mean of  $550 \pm 30$  kg m<sup>-3</sup> for 50 density measurements (both snow and firn) taken in eight pits during the middle of the ablation seasons in 1983 and 1984 (Brugger 1992). Accordingly this yields a cumulative volume change for 2003–11 of  $-28.1 \pm 2.6 \times 10^6$  m<sup>3</sup> where the stated uncertainty includes those in area  $(\pm 1\%)$ ,  $b_n$  [±0.1 m w.e., this being based on analyses by Brugger (1992); cf. Jansson (1999)] and density (±50 kg m<sup>-3</sup>). No attempt was made to account for the slight mismatch of the beginning and ending dates of the balance interval and those of the dGPS surveys. The volume loss that might have occurred after the 2003 survey and before the beginning of the 2003-04 balance year included in our estimate of volume change is thought to be comparable to that occurring after the 2011 survey and before the end of the 2010-11 balance year that is not included in our results.

The values of  $\Delta V_m$  and  $\Delta V_b$  are in excellent agreement (Table 2). What is notable here is that a fairly complete mass balance record is available for 2003–11, and this is the only interval wherein  $\Delta V_m$ is determined using dGPS techniques and thus eliminates the uncertainties associated with map analyses [see Brugger *et al.* (2005) for a brief discussion]. The agreement of  $\Delta V_m$  and  $\Delta V_b$  furthermore implies that the present, rather modest program on Rabots glaciär is sufficiently accurate in determining the glacier's mass balance and documenting volumetric changes.

To explore the robustness of the relationship between  $\Delta V_m$  and  $\Delta V_b$  for the earlier three intervals we use values for the former reported previously by

Table 2. Changes in the volume of Rabots glaciär based on measured changes in surface elevations  $\Delta V_m$ , those estimated using a mass balance approach  $\Delta V_{bs}$ , and mean specific net, winter, and summer balances for select intervals between 1959 and 2011.

Interval	$\frac{\Delta V_m^*}{(10^6 \text{ m}^3)}$	$\Delta V_b^{\dagger}$ (10 <sup>6</sup> m <sup>3</sup> )	$\overline{b_n}^{\dagger}$ (m w.e.)	$\overline{b_w}^{\dagger}$ (m w.e.)	$\overline{b_s}^{\dagger}$ (m w.e.)
1959–1980	$-51.1 \pm 6.0$	$-61.0 \pm 6.0$	-0.61	1.00	-1.61
1980–1989	$-10.4 \pm 7.0$	$-14.1 \pm 2.0$	-0.32	1.13	-1.45
1989–2003	$-14.4 \pm 7.0$	$-22.0 \pm 3.0$	-0.33	1.26	-1.59
2003–2011	$-27.6 \pm 2.6$	$-28.1 \pm 3.0$	-0.84	1.09	-1.93

\* Data for 1959, 1980, 1989, and 2003 from Brugger et al. (2005).

<sup>†</sup> Values might use, in part or in whole, a reconstructed record (see text for discussion).

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Fig. 6. Comparison of estimates of  $\Delta V$  derived from measured changes in glacier surface elevations  $(\Delta V_m)$  with those derived using a mass-balance approach  $(\Delta V_b)$ . Error in  $\Delta V_b$  values is taken at ±10% based on quantifiable uncertainties, but is likely to be larger. Diagonal dashed-line indicates complete concordance. Numbers refer to intervals associated with each data point.

Brugger et al. (2005) and determined the latter using Eqn (1). Figure 6a and Table 2 show that in general the agreement is reasonably good, although it might suggest that either the mass-balance approach overestimates, or the values based on elevation changes underestimate the actual volume loss, or some combination of these. However, further comparison of  $\Delta V_m$  and  $\Delta V_b$  is complicated when considering the steps sometimes necessary to estimate  $b_n$ , differences in measuring protocols (i.e. number of stakes, aerial coverage, etc.), potential inaccuracies in the maps, among other things. For example,  $b_n$  values for 1959–80 in particular are entirely based on correlation with those for Storglaciären. It is therefore difficult to say which method more accurately records volume changes for Rabots glaciär prior to 2003.

#### Longer-term trends in ice retreat and volume loss

The current rate of ice retreat  $(13.1 \pm 0.1 \text{ m a}^{-1})$  is comparable to the mean rate of  $10.2 \text{ m a}^{-1}$  $(\sigma = 2.6 \text{ m a}^{-1})$  of a trend that began *c*. 1933 (Table 1; Fig. 7a). Terminus behavior is largely controlled by longer-term variations in ice flux from upglacier caused by dynamic adjustments made in response to climatically induced changes in mass balance. The lag in propagation of flux variations to

the terminus gives rise to a glacier's reaction time, or length response time (Oerlemans 2001). However, on shorter timescales local mass and energy balances, among other factors, can affect terminus behavior. For example, a particularly severe melt season(s) could result in substantial ice loss at the terminus that depending on its geometry could appear as an interval of anomalous retreat. Conversely inordinate snow accumulation could mitigate, albeit temporarily, retreat. In an attempt to distinguish between these factors, both the magnitude and rate of ice recession for the 12 intervals during the period 1910-2011 (Table 1; Figs 3 and 7a) were compared with mean summer (June, July, August) temperatures for the same intervals either recorded at, or reconstructed for, the Tarfala Research Station located less than 10 km away from the glacier (Fig. 7b). (It bears mentioning here that temperature measurements in the Rabots valley only exist for the summer months of 1984 and for a few weeks in 2003. These measurements correlate very well with those at Tarfala, and suggest mean temperatures in the Rabots valley are on the order of 0.5°C lower.) No correlation exists between the magnitude or rate of ice recession and temperature  $(r^2 = 0.04 \text{ and } 0.09 \text{ respectively})$ . Similarly the magnitude or rate of ice recession for these intervals is not correlated to the mean of the corresponding annual mass balance ( $r^2 = 0.07$ ). In addition, neither are these correlated to glacier-wide mean winter balance  $b_w$  ( $r^2$  for both being ~0.2) that is used here as a surrogate for snow accumulation at the terminus. (Given the typical linear nature of the winterbalance profile over the glacier's lower reach, accumulation at the terminus would approximately scale with  $b_w$ . Note that winter balances for Rabots glaciär prior to the 1981-82 balance year were again obtained via regression of existing values with those from Storglaciären; n = 27,  $r^2 = 0.69$ , p < 0.01; no data for two years.) Thus shorter-term terminus behavior does not seem to be unduly influenced by variations in local energy and mass balances. Nor did any changes in bed or ice surface slopes (both relatively constant) affect terminus behavior during retreat from the glacier's maximum extent. (The possible exception here being the glacier's retreat over a preexisting moraine during the 1950s.) This suggests that the terminus is responding predominantly to the glacier's longer-term dynamic response to a mean (summer) warming trend of ~0.004°C a<sup>-1</sup> defined by 1910–2010 composite temperature data shown in Fig. 7b, or alternatively ~ $0.005^{\circ}$ C a<sup>-1</sup> for only the 1946–2010 temperatures



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Fig. 7. (a) Terminus retreat and rates of retreat for Rabots glaciär 1910–2011. Gray bars distinguish measurement intervals. (b) Composite temperature record for Tarfala Research Station. Temperature data from 1946 to 2010 (solid thin line) were recorded at the station. Earlier temperature data (dashed line) are based on a correlation between the Tarfala Research Station temperatures and a reconstructed temperature series for Tornedalen (n = 57,  $r^2 = 0.73$ , p < 0.001; see Klingbjer and Moberg (2003) for details). Smoothed temperature variation (thick line) uses an averaging window of 5 years. (c) Volume changes based on geodetic measurements, mass-balance data, and a volume-area scaling. Gray bars distinguish intervals. Pertinent data for each interval are also summarized. Error bars are omitted for clarity.



Fig. 8. (a) Correlation of the rate of volume change dV/dt based on measured changes in surface elevations and mean specific mass-balances for the intervals of 1959–80, 1980–89, 1989–2003, and 2003–11. Numbers adjacent to data points indicate the interval. (b) Deviation of mean specific winter and summer balances for the same intervals from their 1959–2011 mean values. (c) Deviation of yearly specific winter and summer balances for the interval d() resulting synthetic record of dV/dt compared with dV/dt expected if either winter or summer balances were constant (see text for discussion).

recorded at Tarfala. This is not surprising in view of the glacier's long length response and volume response times that are respectively 105 and 215 years (Brugger 2007). As noted previously, the glacier's long-term retreat might be somewhat moderated by the apparent increase in winter precipitation that is reflected locally by a slightly increasing trend of winter balances of Storglaciären (~0.006 m a<sup>-1</sup>) and Rabots glaciär (~0.005 m a<sup>-1</sup> using a composite record of  $b_w$ ), for the 1945–2011 observational interval.

Figure 7c also shows the longer-term trend(s) in volume change for Rabots glaciär. Since 1959, measurements indicate glacier volume was reduced by  $\sim 103.5 \times 10^6$  m<sup>3</sup>, or as much as  $125.2 \times 10^6$  m<sup>3</sup>

based on the mass-balance record. As expected, the rates of change in ice volume for discrete intervals are closely related to variations in glacier mass balance. Rates of volume change  $dV_m/dt$  for 1959–80, 1980–89, 1989–2003 and 2003–11 show a very good correlation (n = 4,  $r^2 = 0.99$ , p < 0.005) with the mean annual net balances  $b_n$  computed for the corresponding intervals (Fig. 8a; Table 2) and furthermore corroborates the contention regarding the accuracy of the current mass balance program on Rabots glaciär.

More significantly and in contrast to terminus retreat, it is clear that an accelerated rate of volume loss of  $\sim 3.5 \times 10^6$  m<sup>3</sup> a<sup>-1</sup> began after 2003. This rate is appreciably larger than any that can be docu-

mented for earlier intervals and is approximately double the 1959–2003 average of  $1.7 \times 10^6 \text{ m}^3 \text{ a}^{-1}$ . This increase occurred during an interval characterized by a sharp reduction in mean net balance resulting from significantly less-than-average summer balances  $b_s$  in combination with winter balances  $b_w$ (Fig. 8b) that appear to have been quite typical of those between 1959 and 2011. Greater-thanaverage winter balances for the previous interval of measurement (1989-2003) in combination with slightly less negative summer balances resulted in a substantially lower rate of volume loss of  $-1.03 \times 10^6$  m<sup>3</sup> a<sup>-1</sup>. (Interestingly, a notable difference between the mean summer balances for 1989-2003 and 2003–11 exists despite the mean summer temperature being virtually the same, reflecting the inability of temperature alone to represent the full energy balance involved in ablation processes.) For the interval 1980-89, the mean winter balance shows a small positive deviation from the 1959-2011 average, but the rate of volume loss during this period remained low  $(-1.16 \times 10^6 \text{ m}^3 \text{ a}^{-1})$  in conjunction with considerably less negative summer balances. Despite unremarkable differences in summer balances with respect to the mean, an overall deficit of snow accumulation between 1959 and 1980 (possibly more characteristic of drier conditions at that time?) brought about a rapid rate of volume change of  $-2.4 \times 10^6$  m<sup>3</sup> a<sup>-1</sup>. This underscores how relatively modest, short-term changes or departures in summer balances and/or winter balances can significantly impact the rate of volume change, all else being equal.

> To better quantify the relationship and sensitivity of variations in dV/dt to those in winter and summer balances we use

$$\frac{dV}{dt} = 5.07\overline{b_w} + 4.41\overline{b_s} - 0.45 \tag{2}$$

derived by multiple linear regression (n = 4,  $r^2 = 0.99$ , p < 0.1), where the overbars indicate interval means. As before, summer balances prior to 1981 again obtained via correlation with those on Storglaciären (n = 27,  $r^2 = 0.64$ , p << 0.001). Equation (2) allows us to separate the effect of variations of winter and summer balances (Fig. 8c) on dV/dtby assuming a constant summer and winter balance respectively ("controls"). This analysis is also motivated by the question of whether the latest calculated rate of change in volume (2003–11), that seems quite high for what can be documented, might be unprecedented. Toward these ends, we calculate values of dV/dt averaged over an eightyear moving window for 1959–2011 (the period for which *measured* volume change data exist) using the 1959–2011 mean of the control (1.10 m w.e. for  $\overline{b_w}$  and -1.62 for  $\overline{b_s}$ ) and the window mean for the variable. We specifically use an eight-year smoothing window because this corresponds to the length of the 2003–11 measurement interval, but it bears mentioning that our results are qualitatively the same for other window sizes (e.g. 5- and 10-year).

Despite the shortcomings in using regressionderived values for mass balance components prior to 1981, the results (Fig. 8d) suggest that a sustained interval of volume loss comparable to that of 2003–11 might have occurred during the late 1960s and early 1970s. This period was characterized by both less positive winter balances and more negative summer balances with respect to their mean 1959-2011 values (Fig. 8c), and Fig. 8d suggests that both components contributed to volume loss at this time (i.e. neither alone predicts the expected rate of volume change). An interval of positive values for dV/dt (volume increase) between the late 1980s and the mid-1990s can be largely attributed to substantially increased winter balances aided in part by somewhat less negative summer balances. Part of this interval is reflected in measured volume changes between 1989 and 2003 when the lowest rate of volume loss can be documented. Apparently an overall trend of increasingly negative rates of volume change began prior to the 2003-11 measurement interval. It appears this initially coincides with both a rather sharp decline in winter accumulation - from the significantly higher-than-average amounts in the preceding years - and increasingly negative summer balances. More significantly, however, Fig. 8d suggests that the continuation of this trend to the more recent high rate(s) of volume loss, both measured and derived through Eqn (2), can be attributed almost entirely to persistent arguably extraordinarily so - very negative summer balances. To a large degree, these balances are undoubtedly related to the higher temperature during this time as regression of  $b_s$  on mean summer temperature reveals a significant inverse relationship between these two variables (n = 27, n) $r^2 = 0.54$ ,  $p \ll 0.01$ ) but here again temperature alone fails to fully account for ablation.

Given this longer-term context of glacier behavior the recent increase in the rate of volume loss, if continued, might mark the glacier's response to accelerated warming evident in northern Sweden for the years 2000–10 (Callaghan *et al.* 2010). The

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work presented here and previously (Brugger *et al.* 2005; Brugger 2007) clearly demonstrates that Rabots glaciär is nowhere near steady state. In particular, Brugger (2007) derived a response time of ~215 years for the glacier. Even if approximate, this would suggest that Rabots glaciär is sufficiently along in its dynamic response to the earlier warming (*c.* 1900) and thus the rate of volume change might be expected to be decreasing as a new steady state is approached. Instead the magnitude of volume loss has increased, and this appears to be a consequence of the glacier's response to the most recent temperature increase superimposed on its ongoing response to the earlier warming.

#### Conclusions

Successive dGPS surveys reveal changes in the geometry of Rabots glaciär that occurred between 2003 and 2011. The terminus of the glacier retreated 105 m, equivalent to a rate of ice recession of ~13 m a<sup>-1</sup>. The present rate of retreat is comparable to the longer-term mean established in 1933, presumably after an initial lag in the glacier's response to concomitant regional warming and slower reaction of the terminus beginning in 1910 (Brugger et al. 2005). Between 2003 and 2011 the glacier's surface was lowered by an average of  $7.3 \pm 5.5$  m. The associated volume loss during these eight years was  $27.6 \pm 3 \times 10^6$  m<sup>3</sup>. Volume loss estimated by considering the glacier's mass balance for the same period is  $28.1 \pm 3 \times 10^6$  m<sup>3</sup>. The agreement of these two estimates provides some confidence that current mass-balance measurements (and program) are adequate in documenting changes in the glacier's mass and volume. Volume loss between 2003 and 2011 occurred at a mean rate of  $3.5 \times 10^6$  m<sup>3</sup> a<sup>-1</sup>. Unlike the glacier's retreat, volume (hence mass) loss appears to have accelerated after 2003, the measured rate of change being substantially greater than any time in the past for which it can be quantified. This pronounced increase in volume loss is clearly linked to more negative summer balances and is thought to reflect the glacier's response to a recent temperature increase (Callaghan et al. 2010) superimposed on its ongoing response to the earlier warming. Future research will focus on numerical modeling designed to test this hypothesis.

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